Advancing catchment hydrology to deal with predictions under change

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Abstract

Throughout its historical development, hydrology as an engineering discipline and earth science has relied strongly on the assumption of long-term stationary boundary conditions and system configurations, which allowed for simplified and sectoral descriptions of the dynamics of hydrological systems. However, in the face of rapid and extensive global changes (of climate, land use etc.) which affect all parts of the hydrological cycle, the general validity of this assumption appears doubtful. Likewise, so does the application of hydrological concepts based on stationarity to questions of hydrological change. The reason is that transient system behaviours often develop through feedbacks between the system constituents, and with the environment, generating effects that could often be neglected under stationary conditions. In this context, the aim of this paper is to present and discuss paradigms and theories potentially helpful to advancing hydrology towards the goal of understanding and predicting hydrological systems under change. For the sake of brevity we focus on catchment hydrology. We begin with a discussion of the general nature of explanation in hydrology and briefly review the history of catchment hydrology. We then propose and discuss several perspectives on catchments: as complex dynamical systems, self-organizing systems, co-evolving systems and open dissipative thermodynamic systems. We discuss the benefits of comparative hydrology and of taking an information-theoretic view of catchments, including the flow of information from data to models to predictions.

In summary, we suggest that the combination of these closely related perspectives can serve as a paradigm for the further development of catchment hydrology to address predictions under change.

1 Introduction

Introductory remark: Please note that several terms used frequently throughout the paper are defined in Table 2; their first occurrence in the text is indicated by an asterisk “∗”.

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1.1 Hydrology and change

Man and water co-exist in a tightly knit relationship: Water is an indispensable resource and the basis for human life, but it also poses threats, either by excess, shortage or poor quality. As a consequence, humans have long since struggled to conform natural water availability to their needs, with such prominent historical examples as the Egyptian, Greek and Roman aqueducts, the levees along the Rhine and Danube built for flood protection in the late middle ages, or the centuries-old runoff harvesting techniques used in India (Gunnell and Krishnamurthy, 2003). From practical questions of how to ensure water availability and protection, hydrology developed into an engineering discipline, providing tools for design flood estimation, flood forecasting, and estimation of water availability, etc.

Meanwhile, being one of the most prominent closed loop processes on our planet, the water cycle has also sparked considerable scientific interest, as it plays a major role in global energy and mass cycling (Kleidon, 2010) and connects, like no other, the abiotic environment with the bio- and anthropospheres, thereby governing the distribution of life on the planet. This interest led to hydrology developing into a scientific discipline in its own right, with aims to analyse and describe the phenomena, structures, and processes of the global water cycle.

The dual engineering-science foci of hydrology, along with the multitude of questions, domains and spatiotemporal scales of interest, has led to a diversity of paradigms*, scientific theories*, scientific laws*, and approaches. What unites most of these, however, is an underlying assumption of “stationarity” in regards to most (if not all) of the boundary conditions and system properties; e.g. stationarity of climate, flow regimes, ecosystem function, catchment and river morphology, etc. While this assumption has, to-date, been helpful in simplifying the search for solutions to many hydrological problems, its general validity is increasingly doubtful, one major reason being the ever-increasing influence of man.
There is, now, very little doubt that man plays an important role in global warming and the related changes to global climate (Oreskes, 2004; IPCC, 2007), thereby triggering a chain of changes that propagate throughout the water cycle. To name just a few: (i) shifts in atmospheric circulation patterns affect the annual and seasonal characteristics of rainfall (Bárdossy and Caspary, 1990), (ii) glacial retreat due to global warming affects river flow regimes (Huss, 2011), (iii) increasing water temperature in lakes alters the regimes of thermal layering and aeration (and hence water quality) and favours the invasion of new species (Werner and Mörtl, 2004), and (iv) rainfall regimes at the regional scale are influenced by human strategies for rainfall enhancement (Griffith et al., 2009).

Comparable in impact to the changes in global climate, man-made changes in land use affect all aspects of the water cycle around the world, which in turn alter weather and climate from local to regional scales. Altogether, croplands and pastures have supplanted natural vegetation to become one of the largest terrestrial biomes on the planet, now occupying 40% of the land surface (Foley et al., 2005), and an estimated 60% of present soil erosion yields are induced by human activity (Yang et al., 2003). Arguably the most dramatic example of human influence on regional hydrology is the Aral Sea, where withdrawals of water (for irrigation) from the 1.5 million km$^2$ basin have led to a massive shrinkage and desiccation of the lake, extinction of the aquatic ecosystem, and reduction of regional rainfall to one third of its initial value and lake inflow to one sixth (Gaybullaev et al., 2012). Another interesting example is the fact that 55% of Dutch land would be under water if it were not for the dykes built by man (IPCC, 2007; Corrigendum to IPCC). Last, but not least, urbanization has had a major effect on local and regional regimes of water and sediment flows and on fluvial morphology (Hawley and Bledsoe, 2011), with the consequence that aquatic life cycles, habitats and food webs have been altered (Poff et al., 2006).

To summarize, the hydrological cycle is increasingly affected by changes, many of them triggered by humans, which extend from the local to global scales, act on short to decadal time scales, affect all characteristics of water-related dynamics (mean, variabili-
ity, extremes), and extend over the atmosphere, critical zone (boundary layer), groundwater, lakes, rivers and oceans.

1.2 Hydrological complexity and co-evolution

Taking the perspective of systems theory, hydrology deals with an overwhelmingly complex, non-linear coupled system, with feedbacks that operate at multiple spatiotemporal scales (Kumar, 2007; Sivakumar, 2009). The fact that aspects of the hydrological system have been successfully dealt with in greatly simplified ways (through isolated treatment of sub-systems and linearized approximation of dynamics), while neglecting many of the feedbacks, is made possible mainly by the fact that long term co-evolution of the various system components (morphology, vegetation, river networks, etc.; see Corenblit et al., 2011) has resulted in stable system configurations, wherein stabilizing negative feedback effects govern the system dynamics, so that the system degrees of freedom are greatly reduced.

For such systems, the net effect of the past interplay of feedbacks has become engraven in the system configuration, so that many of the system-shaping feedback processes need not be explicitly included in a representation of system dynamics. However, when such systems are forced sufficiently far from these stable quasi-steady states*, either by changing the boundary conditions or system properties, system reconfigurations towards new, unexpected and potentially unpredictable transient* and stable states may be triggered (Phillips, 1993, 2006). As the nature of the new system configurations will be largely governed by the interplay of positive and negative feedbacks, limits to the applicability of hydrologic solutions based in the stationarity assumption quickly become obvious.

1.3 Goals and scope of this paper

This so-called “end of stationarity” therefore poses a grand challenge to hydrology, which has recently been acknowledged (among other initiatives) by the IAHS, devoting
the decade 2013–2022 “Panta Rhei” (Montanari et al., 2013) to “predictions under change”, PUC (Sivapalan, 2011; Thompson et al., 2013). Therefore, in the context of this IAHS initiative, the main aim of this paper is to present and discuss paradigms and scientific theories which we believe will be helpful in advancing hydrology towards understanding and predicting the behaviour of hydrological systems under change.

To be clear, this paper is intended to serve primarily as an overview, while many of the topics we identify are dealt with in greater detail within this special issue; we will point to them where appropriate. PUC questions pose both a challenge and an opportunity for the science and practice of hydrology. Because of the increasing need to jointly consider hydrological system components with processes from the abiotic environment, and the bio- and the anthroposphere across many scales, we are afforded the opportunity to begin a unification of the still fragmented landscape of hydrological theories and approaches into a more comprehensive framework. The second aim of this paper, therefore, is to discuss the structure and components of such a framework and to examine what role each of the paradigms presented may play within it.

For the sake of focus we will limit the paper to the topic of “catchments”, these being the most important and intuitive conceptual hydrological construct, although many of the paradigms presented here will also be applicable to other hydrological sub-systems (e.g. groundwater) and to the global hydrologic cycle.

The remainder of the paper is structured as follows: We begin with some general definitions and an overview of the nature of explanation in hydrology (Sect. 2). Then we present a historical perspective on the development of hydrology, discuss where it stands today and consider whether the methods it offers are suited for questions dealing with PUC (Sect. 3). In Sect. 4, we briefly discuss a number of paradigms and theories that we believe will be helpful for understanding the nature of catchments under change; these include the theory of complex dynamical systems (Sect. 4.1), catchment self-organisation, co-evolution and similarity (Sect. 4.2), thermodynamics (Sect. 4.3) and information theory (Sect. 4.4). In Sect. 5, we summarize and conclude
with a discussion of how the various paradigms presented here may contribute to the development of a general framework for the science of hydrology.

2 The nature of explanation in hydrology

Which scientific approaches and methods do hydrologists use to describe, explain and predict hydrological phenomena and why?

In this section, we will discuss the general ways of explanation used in hydrology. This provides the ground upon which to discuss how problems associated with hydrological change can be approached, and to identify which currently available methods may be potentially useful for addressing them.

It is important, first, to recognize that “explanation” in hydrology is characterized by a considerable degree of pluralism, as it does also within the earth sciences in general (this paragraph largely draws from Kleinhans, 2005). This pluralism stems from different types of explanation, and the interdisciplinary and underdetermined nature of hydrology, as we will discuss below. In general, we can distinguish three co-existing types of explanation:

1. Descriptive actual-sequence explanations of the course of (unobservable) sequences of past events such as soil genesis (Buol et al., 2011), paleoflood reconstruction (Baker, 1987), long-term reconstruction of fluvial morphology (Garcia-Garcia et al., 2013) or land-use and climate (Ropke et al., 2011).

2. Robust-process explanations that provide cause-and-effect relations without going into detail (typically, they are referred to as general mechanisms or process patterns). A typical example from hydrology is the description of the general mechanisms of surface runoff production. Such explanation can be formulated without full knowledge of initial and boundary conditions.
3. **Causal explanations in the form of scientific laws** that provide a detailed description of (typically isolated) mechanisms and the exact ranges of applicability, in which they must qualify as exceptionless and irreducible (e.g. Darcy’s law for saturated flow in porous media).

In addition to this, further pluralism arises from the diversity of questions that hydrologic investigations deal with, and from the occurrence of emergent phenomena (see Sect. 4.2.1). These multiple perspectives have, historically, favoured the formulation of laws that apply to specific phenomena and at particular spatio-temporal scales. Going further still, and due to its interdisciplinary nature, explanation in hydrology has also embraced concepts from a variety of disciplines including physics, chemistry, biology, geology, ecology and systems theory, and increasingly relies on quantitative computer models (Oreskes, 2003) for analysis, explanation, forecast*, prediction* and projection*, despite their many limitations (Oreskes et al., 1994).

This high degree of explanatory pluralism in hydrology is, we believe, an obstacle to the further development of the science, as it hampers communication and cooperation among its sub-disciplines. However, the main reason for its existence, that being “underdetermination”, is likely to be difficult to overcome. Here, the term underdetermination is used for “the lack of sufficient data to formulate complete causal explanations, caused by the impossibility of complete observation (e.g. in the subsurface or due to long process time scales) and of undisturbed observation”. This situation is, of course, complicated by the fact that many hydrological systems exhibit strongly nonlinear behaviour and have unknown boundary and initial conditions. Together, this imposes principal limits on our ability to make (deterministic) predictions (Koutsoyiannis, 2010). So the important question that arises is:

*How can we cope with underdetermination and reduce explanatory pluralism in hydrology?*
This has been a longstanding issue, but it has now become even more relevant when faced with the need to address questions of hydrological change. When systems are changing, we can be quickly confronted with a diminished ability to predict the future based purely on past observations, due to the potential invalidation of steady-state\textsuperscript{*} laws.

From a methodological point of view, one useful approach to diminishing the problem of underdetermination is to attempt to combine knowledge contained in actual- and robust-process explanations with laws in a hierarchical way, i.e., locally valid laws can be tested to establish robust-process predictions on a larger scale, and robust-process explanations can be tested against long-term developments of the system. In this paper, such an approach is reflected in our suggestion to view catchments both as (i) systems of many component sub-systems that self-organize on the basis of locally valid laws (Sect. 4.2.1) and (ii) as co-evolving entities (Sect. 4.2.2). We suggest that a key to explaining self-organization and emergence is to treat catchments as open dissipative thermodynamic systems (Sect. 4.3), which can thereby provide a hierarchical framework in which sectoral laws based on emergent phenomena can be placed. It is also a framework in which limits to the intensity of processes can be formulated.

While considering the above suggestions, it is perhaps helpful to recognize that algorithmic information theory (AIT), offers a complementary (albeit more idealized and philosophical) view of the nature of explanation, data, models and laws. AIT is based on the perspective that all data, models and laws can, in principle, be represented as algorithms on some universal elementary computer (Solomonoff, 1964; Chaitin, 1966; Kolmogorov, 1968). When approached from this point of view, an “explanation” is simply a useful form of “data compression” which enables a description of some aspect of the system in a much shorter form (requiring less storage), and a “theory” or “law” is a useful “computer program” that is capable of generating the observed data as output (Weijs et al., 2013a,b). If a theory is able to represent the nature of the structure\textsuperscript{*} in some observed data, then the computer program representing it (the new description) should require less storage than the original data (original description). This quantifies
the principle of parsimony by means of information measures. The main implication of this framework is that the “why” questions of science are, at a fundamental level, really secondary to the “how” questions, since any explanation of an observed phenomenon (“why”) consists of a description (“how”) at a deeper level (Feynman, 1965).

It is also useful to realize that AIT is closely linked to Bayesian probability and the classical information theory (IT) of Shannon (1948). What makes it attractive as a basis for scientific investigation is that (A)IT offers a general framework for the evaluation of information content (expressed in terms of the reduction of uncertainty about a target quantity of interest), across data, laws, and models. Importantly, it reminds us that the information content of any data, law or model depends critically on the question being asked and on the nature of the prior knowledge available. Accordingly, the best current explanation necessarily depends on the information currently available. These insights are particularly important to the investigation of hydrological phenomena, where underdetermination leads to a strong reliance on model-based hypothesis testing, analysis and prediction across scales. A more detailed treatment of (A)IT is presented in Sect. 4.4.

3 Catchments and catchment hydrology

The existence of catchments is the blessing and curse of hydrology and it has had a major impact on its historical development. To illustrate this, we will discuss what a catchment is, sketch the historical development of the science of catchment hydrology and, from this, take a look into its future.

3.1 What is a catchment – characteristics and peculiarities

The predominant feature of a catchment is its convergence into a stream channel. This allows the total outgoing flux of surface runoff to be readily measured, which, in turn, allows straightforward closure of the catchment water mass balance. This water
balance equation has so far proven to be the most useful physical principle in hydrologic analysis, and it greatly facilitates the estimation of harder-to-observe fluxes such as evapotranspiration. The second interesting characteristic of a catchment is that the processes associated with landscape and soil formation operate at much longer time scales than do rainfall, evapotranspiration and the shallow water flow that contributes to most of the runoff (e.g. Skøien et al., 2003). Similarly, changes in land use typically occur relatively slowly as do changes in stream morphology. This allows a treatment of catchment dynamics in which slow and fast time scales are separated (Blöschl and Sivapalan, 1995), thereby transforming a complex problem into two simpler ones, and avoiding the explicit representation of feedbacks between system states (e.g. soil moisture) and catchment structure (e.g. topography) (Gaál et al., 2012). For example, in hydrological modelling, it is often conveniently assumed that the variables representing climate vary in time while the general model structure and the model parameters representing catchment characteristics remain time-invariant (Merz et al., 2011; Blöschl and Montanari, 2010).

An interesting consequence of this separation of time scales is that hydrological models have, historically, been “tuned” to remove bias via calibration (Gupta et al., 1998, 2008; Blöschl et al., 2013). The ability to separate slow and fast time scales can also be found in other disciplines such as meteorology, where short time scales are associated with atmospheric motion and long scales with e.g. ocean and ice dynamics (Hasselmann, 1976). If, however, the spatio-temporal scales of interest are close to those of structure formation and decay, then more constraints, such as the mass- energy- and momentum balances are required to allow solution of the dynamical system equations. A typical example from meteorology is local weather forecasting including the formation of local convective structures. In catchment hydrology, time scales of interest are typically such that a separation of scales, and with it a simplified treatment of dynamics, is possible.
3.2 The historical development of catchment hydrology research

The characteristics of catchments discussed above have been a strong motivation for hydrologists to look at hydrological processes from a catchment perspective. Equally important, many societal problems that hydrologists have had to solve occur at the catchment scale, giving additional impetus for a catchment scale perspective. Indeed, when looking back in history, it is clear that the evolution of hydrology has been mainly driven by the societal problems of water management and risk (Nash et al., 1990; Eagleson, 1991). As hydrology is a broad discipline, we will discuss its historical evolution only from the viewpoint of flood modeling, which is of interest both from a theoretical and practical perspective.

The first approaches to model the dynamics of streamflow volume, such as the Rational Method (Mulvany, 1850) and the Unit Hydrograph concept (Sherman, 1932; Dooge, 1973) mainly adopted assumptions of linearity and time invariance, and were developed at the event-scale, lumped for the catchment. Early in the 20th century, questions of agricultural management led to the integration of soil moisture dynamics in the models, thus introducing the first major representation of interactions/feedbacks (between evaporation, soil moisture and runoff) and the gradual move towards higher temporal resolution, eventually resulting in lumped catchment-scale models such as the Stanford Watershed Model (Crawford and Linsley, 1966), the Sacramento model (Burnash et al., 1973) and the HBV model (Bergström, 1976). Meanwhile, quite isolated from these developments and motivated mainly by flood frequency analysis, flood hydrology also developed a strong statistical branch (Kritsky and Menkel, 1946; Gumbel, 1941; Merz and Blöschl, 2008).

This was soon followed by models with increasing spatial resolution (see the blueprint of Freeze and Harlan, 1969), based on local-scale equations (e.g. SHE, Abbott et al., 1986), and making use of the growing knowledge on hydrological processes and availability of spatially highly resolved data. Until today, the development continues towards more complex water balance models involving vegetation dynamics (e.g.
LARSIM, Ludwig and Bremicker, 2006) or SVAT models in the context of climate modelling (e.g. CLM, Dai et al., 2003), with increasing representation of within-catchment feedbacks and land-atmosphere interactions. Over decades, discussions have taken place on (i) how to obtain estimates for the model parameters of these kinds of models given the complexity of the processes in the landscape (Gupta et al., 1999; Hogue et al., 2006; Rosolem et al., 2012) and (ii) whether the assumed model structures are appropriate in the first place (Beven, 1989; Grayson, et al., 1992). Much of the difficulty is related to scale issues, the fact that laboratory equations cannot be straightforwardly extended to the catchment scale, and the difficulty with measuring model parameters in the field at the appropriate scale (Blöschl and Sivapalan, 1995). Advances in measurement techniques, in particular about spatial patterns (e.g. Grayson et al., 2002), helped address the dispute as they provided new information to identify at least some of the model parameters. The discussion on what scale best to formulate hydrological processes, however, has not been resolved.

On the whole, the existence of catchments has been a blessing for hydrology, by enabling the development of relatively simple but successful models based on the assumptions of stationarity, linearity concepts and the availability of very few observations. On the other hand, this has also slowed the development of models that properly represent the true complexity of water-related processes along the hydrological cycle and that simulate the interplay of short- and long-term dynamics.

However, it is the latter kind that is increasingly required to deal with catchments under change, wherein the assumption of stationarity (or more generally the assumption of separation of time scales) must be relaxed. In the next section, we will examine several perspectives on catchments that will potentially be useful to direct the further development of hydrological models to approach such questions of change.
4 Perspectives on catchments under change

4.1 Catchments as complex dynamical systems

The first perspective we take is that of catchments as complex dynamical systems. The theory of dynamical systems is a well-established branch of science that has been proven useful across a wide range of problems and systems (Strogatz, 1994) ranging from weather prediction (Lorenz, 1969), ecology (Hastings et al., 1993) and hydrology (Koutsoyiannis, 2006) to geomorphology (Phillips, 1993) among many others. The steps of Dynamical System Analysis (DSA) include identification of the system structure (border, components, and state variables) and of the laws governing its dynamics (i.e. the evolution of system states over time). A major strength of DSA is that it offers a method for system classification based on its degrees of freedom (state variables) and the nature of its dynamics (linear, non-linear, chaotic, see Table 1), which allows conclusions to be made on system stability and predictability.

Although there is, to date, no consensus regarding an exact definition of what characteristics define the special class of complex dynamical systems, several constituent features are generally accepted (Heylighen, 2008; Sibani and Jensen, 2013). These include strongly nonlinear and possibly chaotic behaviour, resulting from the combinatorial effects of damping/amplifying feedbacks and interactions between sub-systems, the occurrence of emergent behaviour, limited predictability and the potential for self-organisation in Ashby’s terms (Ashby, 1962; see also Sect. 4.2.1). Accordingly, catchments qualify as complex dynamical systems: Hydrological processes exhibit non-linearity over a wide range of spatio-temporal scales, from micro-scale fingering in soil water infiltration (Ritsema et al., 1998) to the Hurst–Kolmogorov behaviour of hydrological processes on the climatic scale (Montanari et al., 1997; Koutsoyiannis et al., 2009), which can lead to high sensitivity to initial and boundary conditions and potentially to chaotic behaviour (Sivakumar, 2000). In addition, catchments exhibit emergent behaviour (see Sect. 4.2.1), changing patterns of stable and unstable states (Dooge, 1986; Brandes et al., 1998; Zehe et al., 2007), complexity of sub-system behaviour...
at different scales (Zehe and Blöschl, 2004; Rodriguez-Iturbe et al., 1991) and varying sub-system memory (e.g. residence times in rivers typically on the order of days, whereas in groundwater systems it may be decades).

More specifically, according to the definitions of Weinberg (1975), hydrological systems are often systems of intermediate complexity and organization (Dooge, 1986). Existing between the realms of organized simplicity (mechanisms) on the one hand and unorganized complexity (aggregates) on the other implies that hydrological systems can neither be fully described and predicted by methods of deterministic mechanics (as for mechanisms) nor by statistical physics (as for aggregates). Hydrological systems, as systems of “organized complexity”, exhibit a mixture of both dimensions, being roughly predictable under some conditions and at certain scales but unpredictable at others. Waldrop (1992) termed such systems as being at the “edge of chaos”. In this context, DSA may prove useful for hydrology science by providing the tools (Strogatz, 1994) for constructing a required “concept of reality intermediate between determinism and randomness in which changing patterns of stability and instability contribute to the self-organization of systems” (Dooge, 1986).

In the context of PUC questions, an important potential of DSA lies in providing a method for classifying hydrological systems with respect to their predictability and, therefore, for distinguishing between predictable and unpredictable systems (one of the “key unresolved issues and research challenges in hydrology”; Blöschl, 2006). A number of studies have been carried out in this context, including (i) identification of patterns of hydrologic predictability (Zehe and Blöschl, 2004; Zehe et al., 2007), (ii) analysis of predictability limits caused by dynamic changes in spatial catchment complexity (Kumar, 2011) and (iii) defining factors affecting global hydrologic predictability (Shukla et al., 2013). Further, DSA can contribute to the identification of patterns of long-term predictability in regional water cycle processes, through division of the system into components of different memory length (Demchenko and Kislov, 2010) similar to approaches used in climate prediction (Hasselmann, 1976). DSA can also be useful for analysing projected scenarios of hydrological change. Conditions can be analysed,
and physical mechanisms detected, which lead to instability of hydrological systems, induction of new stable states, and conversion of former time-invariant structures into time-variable ones, etc. In particular, dynamical invariants (known as the Lyapunov exponents) related to the average rates of divergence or convergence of trajectories in phase space, can be used to quantify the effects of instability, and can thereby serve as measures of stability, resilience, and ultimately predictability of hydrological systems under change.

In the context of addressing PUC questions, some limitations of classical DSA are its traditional focus on systems having time-variable states but time-invariant structure. From a thermodynamic perspective, catchments are open, dissipative, and far from equilibrium, and can experience substantial changes in structure (either build-up or decay, see also Sect. 4.3). Further, DSA does not, by itself, provide answers about whether principles exist that direct the development of catchment structure. Pathways to address these issues will be discussed in Sects. 4.2 and 4.3. Finally, caution should be exerted when estimating the degrees of freedom of a hydrological system. Deriving this number from its number of dependent variables may result in an overestimation, as it may in reality be much smaller due the synchronizing effect of emergence at various scales, (see also Sect. 4.2.1).

To conclude with the words of Dooge (1986), “Generally, systems theory attempts to produce laws that provide insight rather than specific answers”. In accordance with this, we believe that it is these insights that form the potential of DSA for hydrologic science in the context of PUC questions.

### 4.2 Catchments as self-organizing, co-evolving systems

In this section we discuss why, despite the dazzling array of hydrological processes acting at various scales and across many compartments, catchments do not behave as random conglomerates, but instead exhibit a high degree of organisation and structure. In fact it is not *despite*, but rather *because* of the large number of sub-systems and processes that self-organisation and emergence can take place (see Sect. 4.2.1) and...
that the interaction of catchment components over time (i.e. co-evolution in the sense of a joint, non-random development) eventually leads to harmonized sets of constituents (see Sect. 4.2.2) that are likely to occur repeatedly given similar initial and boundary conditions. By taking the view of catchments as self-organizing, co-evolving systems and by exploiting catchment similarities to transfer information across space or time (Sect. 4.2.3), it becomes possible to constrain the range of future trajectories of the evolution of a catchment, thereby enabling predictability under change.

4.2.1 Catchments as self-organizing systems

The organization of light waves into coherent laser light, a bowed string emitting sound waves of only a single key and its harmonics, establishment of predator-prey cycles in ecology, and the formation of eddies in fluid flow are all examples of a phenomenon that is ubiquitous in nature – the ability of systems to spontaneously develop macro-scale (macro-scale here refers to a scale similar to the extent of the system) properties or structures (spatial, temporal or functional) from the cooperation of its micro-scale (i.e. much smaller than the extent of the system) constituents (i.e. for the system to become more than the simple sum of its parts). This is fundamentally different from macro-scale properties that simply arise from superposition of the properties of a set of micro-scale constituents (e.g. total mass of a system as the sum of sub-system mass or the linear macro-scale function of a system composed of linear sub-systems). The appearance of such macro-scale structure and hence the establishment of a hierarchy within the system is referred to as emergence, the underlying process self-organisation (Jetschke, 2009). In this context, “organisation” can be thought of as a process leading to conditionality, i.e. the dependence of the value or state of an entity on the state or value of another (Ashby, 1962). Altogether, the notion of self-organisation is reminiscent of Darwin’s concept of evolution (Haken, 1980).

Within the scientific field of synergetics, which is closely related to the theory of complex dynamical systems (see Sect. 4.1) and thermodynamics (see Sect. 4.3), several criteria for the occurrence of emergence have been established (e.g. Haken, 1980).
particular, the system is typically composed of many similar, interacting sub-systems that are subject to external influences. Further, the nature of their interactions can usually be described by a few macro-scale order parameters, which are in turn dependent on external conditions. Depending mainly on the values of these order parameters, the nature of the interactions change (often in an abrupt, threshold-like manner, and caused by a shift from none or negative towards positive feedback effects among the sub-systems) from non-cooperative (non-conditional) to cooperative (conditional) behaviour. Importantly, for an emergent macroscopic property/structure to arise, the temporal persistence of the order parameters must be much larger than the time scale of the cooperative processes. Also, states that are far from thermodynamic equilibrium* are favoured for self-organisation to occur (see Sect. 4.3).

There are many striking examples of emergence along the hydrological cycle: flow fingering (Hill and Parlange, 1972) leads to structured flow at the macro-scale (soil columns), its occurrence being governed by the relationship between soil moisture and the hydraulic properties of soil and fluid. This cooperative effect is caused by a positive feedback between soil moisture and hydraulic conductivity. Similarly, the formation of persistent preferential flow structures in a catchment (e.g. river networks visible at the macro-scale) is governed by just a few order parameters (the degree of convergence of initial geopotential gradients, and the relationship between fluid shear stress and resistance to soil erosion), but adds an entirely new function to the system. In this case, the conditional (positive feedback) mechanism is related to the locally steepened gradients (towards the channel) and the reduced flow resistance (in the channel); see also Kleidon et al. (2013). Note that the formation of hillslope subsurface stormflow (see Fig. 1 in Troch et al., 2009 or Lehmann et al., 2007) and other kinds of threshold-like behaviour (Ali et al., 2013; Zehe and Sivapalan 2009) can also be seen as resulting from a hierarchy of emergent phenomena.

From the above discussion, it should be clear that hydrologists (and scientists in general) have long taken advantage of emergent phenomena when formulating laws for macro-scale dynamics in systems composed of many sub-systems (with the definition
of the macro-scale being dependent on the specific purpose). However, for hydrological systems that can be viewed as exceedingly complex, and where one has to deal with predictions under change, there still lies considerable potential in the synergetic view. Although it is likely that we will never be able to fully describe such systems in terms of their smallest component entities (in a reductionist sense), a strategy based on making use of emergent phenomena can greatly reduce the degrees of freedom to a manageable number of order parameters, thereby making prediction a more straightforward (and less uncertain) task. It should be noted, however, that while self-organisation typically leads to macroscopically stable (and hence predictably steady) states, such systems can also exhibit complex (even chaotic) dynamics under certain conditions of their order parameters.

The general findings of synergetics have been found to be applicable to a wide range of systems, from physical and chemical to biological and social. As hydrological systems can comprise components from all of these, working within a common framework and language of synergetics has the potential to simplify the transfer of knowledge and improve communication. Further, the fact that self-organisation constrains the degrees of freedom for a catchment to develop is also a reason for the apparent similarity of many catchments (see Sect. 4.2.3). However, despite the potential of exploiting self-organisation, there are many challenges and limitations that should not be ignored; for example, the macro-scale order parameters and their corresponding macro-scale laws must be identified, the ability to make meaningful statements about detailed behaviours at the micro-scale is lost, and the effects of self-organisation can only be exploited under the assumption that the system does not change at the micro-scale. The latter may not always be true, especially for catchments under change. If for example the micro-scale soil hydraulic properties in a catchment change due to external influences, previously visible fingering may cease to occur.
4.2.2 Catchments as co-evolving systems

The hydrologic system embedded in a catchment is both a driver and a result of changes in soil, topography, biota and human actions over multiple time scales of history, resulting in striking and remarkable patterns at all spatial scales, as described in the previous section. Hydrologic models that aim to predict the hydrologic functioning of the landscape based on the traditional reductionist or Newtonian approaches, face enormous challenges in finding ways to represent and parameterize the structure of the landscape (Sivapalan, 2005), but entirely ignore the constraints on parameter combinations or self-organization that may reasonably result from the history and co-evolution of the geology, soil, topography, and biota. Despite advances in geomorphology, pedology and ecology in unraveling the pathways and mechanisms that have determined those facets of the landscape, in conventional reductionist approaches the hydrology of a catchment is still largely understood as a system without a history, as brute fact.

The “Darwinian” approach to hydrologic science aims to identify, explain and make use of the patterns of functional diversity in populations of catchments (Sivapalan et al., 2011; Harman and Troch, 2013; Wagener et al., 2013). Charles Darwin’s own profound insights can be traced to his focus on the relationship between individuals and populations, rather than either alone, and in his search for theories that explain patterns of variations in populations in terms of mechanisms that operate on individuals over history (Harman and Troch, 2013). The Darwinian approach to catchment hydrology would echo this focus. The primary data for Darwinian hydrology would likewise combine detailed analysis of the signatures of holistic hydrologic function in individual catchments, and the functional patterns that emerge when many catchments are compared on the basis of functional similarity, giving rise to the notion of comparative hydrology (Falkenmark and Chapman, 1989; Jothisangkoon et al., 2001; McDonnell et al., 2007; Blöschl et al., 2013), see also Sect. 4.2.3 on catchment similarity.

The objective is to find generalizable mechanisms of landscape change that apply to a range of places that share broad conditions (Ghiselin, 1969; Kleinhans et al.,
2010; Gupta et al., 2013a). For example, it appears that there is a consistent trajectory of hydrologic evolution in upland basaltic watersheds from groundwater-dominated in relatively young landscapes to shallow subsurface lateral flow in older ones, as the works of Lohse and Dietrich (2005) and Jefferson et al. (2010) indicate. These findings suggest that one may be able to find predictive relationships between the degree of drainage incision (a topographic signature of the older watersheds) and hydrologic partitioning in landscapes with a similar history, which can inform Bayesian priors in model parameter identification.

The coupling between predictions based on co-evolution and particular mechanisms of watershed change suggests that a catchment classification system based on a shared developmental pathway “genotypes”) may be more fruitful than one based on similar current hydrologic behaviour alone “phenotypes”) (see Sect. 4.2.3). Srinivasan et al. (2012) offers a nice recent example of how this type of thinking can be applied to socio-hydrologic questions (Sivapalan et al., 2012).

Approaches for testing such explanatory theories are widely discussed in the geology and ecology literature (Chamberlin, 1890; Rhoads and Thorn, 1996). Darwin himself had great success adopting a hypothetico-deductive approach in which the central hypothesis is used to generate a series of corollary hypotheses (if A is true then B must also be true) that can be compared to subsequent observations, leading to an iterative relationship between theory and observation (Ghiselin, 1969; Mayr, 1991).

Note that it should be uncontroversial to suggest that catchments “evolve” since this simply implies change over time, and says nothing about the mechanism of that change. Similarly “co-evolution” in this context is simply the hypothesis that changes in hydrology, topography, soils, ecosystems and human activities are interdependent. Darwin’s “theory of evolution” was not a proposal that evolution occurs (that idea had been around for centuries) but rather a mechanism for that change that unifies and explains observed patterns of variations in species (i.e. natural selection). Darwinian hydrology could similarly search for ways to unify the variability of catchments’ hydro-
logic behavior, but will have to search for its own mechanisms, since clearly “natural selection” does not apply.

There are links between Darwinian explanations of structure and function and the concept of optimality, which hypothesizes that there exists an “optimal” state towards which a system will evolve (see Sect. 4.3.1). It should be noted, however, that even if such optimal states exist, the Darwinian approach admits that the contingencies of history of a system can strongly constrain its degrees of freedom to evolve, creating lasting sub-optimal forms that dominate current structure (see also Gould and Lewontin, 1979).

Focusing on the historical co-evolution of catchment components is also strongly linked to the thermodynamic and dynamical systems perspective we take in Sects. 4.3 and 4.1: the unique historical trajectory of a catchment can be explained by the appearance of irreversible processes and by the unique path the catchment takes, during its evolution, at points of instability where the results of random processes have an impact on the further development of the catchment.

Rather than a single “new theory”, the Darwinian approach to hydrology aims to develop a body of knowledge and wisdom about landscapes that provides constraints on the current and future unknown parameters (or perhaps on the hydrologic fluxes themselves, bypassing the need for such parameters). This knowledge should be predicated on a set of theories that explain and predict the co-evolution of the hydrologic functioning of the landscapes as a whole, locally dependent on the smaller set of key historical and contemporary forces (climate and geology) that have conditioned and constrained that evolution. In this sense there is a clear need for a synthesis of the traditional Newtonian approaches that involve the study of individual catchments and Darwinian approaches that are based on the comparative study of populations of catchments, as called for in a series of papers culminating in the most recent outcome of the Predictions in Ungauged Basins initiative (Sivapalan, 2005; McDonnell et al., 2007; Sivapalan et al., 2011; Blöschl et al., 2013; Gupta et al., 2013b). The question is open...
whether Darwinian theories and constraints can be found and used to constrain and test predictive reductionist models.

### 4.2.3 Catchment similarity

Catchment similarity, in a hydrologic sense, refers to the question why two catchments exhibit similar hydrologic response characteristics (Wagener et al., 2007). Catchment similarity is the basis for catchment classification, for transferability of information, for generalization of our hydrologic understanding and also for understanding the potential impacts of environmental change (McDonnell and Woods, 2004). The apparent similarity of many catchments around the world is likely rooted in their shared principles that guide catchment evolution over time and on their shared emergent effects (see Sect. 4.2.1). Comparing catchments of presumably common initial and boundary conditions with respect to their dissimilarities therefore gives insight into remaining degrees of freedom, while comparing them with respect to their similarities gives insight into universal constraints of catchment evolution. Typically, this similarity is assessed by estimating the distance between two catchments in a suitably chosen metric space, although careful exploration of the consequences of choices made regarding distance measures and potential clustering approaches is necessary to understand their impact on the similarity analysis results. An overview of techniques and measures to quantify similarity of catchment structure, function and response on various scales is given in Wagener et al. (2007). Blöschl et al. (2013) organize their comparative assessment of runoff predictions in ungauged basins around the notions of catchment, climate and hydrological similarity.

For example, catchments satisfying the Budyko curve (Budyko, 1974) manifest the similarity of long-term hydrologic functions (partitioning of precipitation into rainfall, runoff and evapotranspiration) under stationary climatic controls; while the deviation from the Budyko curve likely manifests the remaining degrees of freedom such as vegetation and landscape variations (Troch et al., 2013). The similarity of climate control on base flow and perennial stream density shows the common constraints on shal-
low groundwater discharge and basic stream network formation (Wang and Wu, 2013). Similarity in geology (e.g. karst versus non-karst) is reflected in the strength with which an incoming precipitation signal is filtered (damped) by a catchment, so that strongly different flow regimes can be observed even under similar rainfall regimes (e.g. Tague and Grant, 2004). Land use will also create hydrologic differences between otherwise similar catchments (similar in pedology, geology, and climate). For example, differences between mature forest and pasture landscapes in neighboring catchments in Mexico become clear under more intense storms (once every 2 yr) (Munoz-Villers and McDonnell, 2013). Under those conditions, the infiltration capacity of the pasture is exceeded and event water contributions are much higher than for the forested landscapes even though both overlay rather permeable volcanic soils.

The difficulty in assessing the degree of similarity and dissimilarity is unfortunately most often complicated through the interaction of multiple physical characteristics (e.g. a mixture of geologies), which does not allow for a very clear separation in many cases. For example, Martin et al. (2012) concluded that the degree of urbanization in US catchments had to exceed about 15 % before hydrological signatures could be differentiated between urbanized and non-urbanized catchments. Given this ambiguity and our limited ability to exactly estimate the physical characteristics of a catchment, it is often necessary to resort to the use of dynamic models in which the physical system is parameterized (Carrillo et al., 2011). As a consequence, we still have to face the widely discussed issues of equifinality and model structural uncertainty.

Searching for hydrologic similarities and their organizing principles can help to estimate the future of existing catchments under changed boundary conditions by trading space for time (Singh et al., 2011). So far, little thorough investigation has been done on this topic and its use in hydrology, which means that the validity of its basic assumptions and its broad value still have to be assessed. For example, under what conditions is spatial variability a proxy for temporal variability?
4.3 Catchments as open dissipative systems far from equilibrium

Since its beginnings with the work of Carnot and Clausius in the 19th century, thermodynamics has been recognized as a fundamental theory about nature (Klein, 1967) and has so far proven to be applicable to any natural system, be it physical, chemical or biological. While its first law essentially states the conservation and convertibility of energy, the second law states that in isolated systems, the entropy of the system can only increase. Entropy is a physical property of the system that describes the extent to which energy is dispersed (unavailable to perform work) within the system. In other words, spontaneous processes always deplete (and never establish) potential gradients, thereby increasing the system’s entropy. The second law describes irreversibility caused by dissipative processes such as heat transfer, friction, chemical reactions and diffusion and hence introduces an arrow of time to natural processes (Eddington, 1928).

Viewing catchments as open, dissipative thermodynamic systems far from equilibrium in the framework of thermodynamics offers several advantages. We will discuss them by first addressing what these terms imply using the example of heat transport in a reservoir heated at the bottom and cooled at the top (the well-known Benard experiment, see Fig. 1): The state of any thermodynamic system can be characterized by a set of macroscopic state variables and a unique stable state termed thermodynamic equilibrium (TE) at which it will arrive in isolation. The reservoir in Fig. 1 is in TE if the temperature gradient between the top \( T_o \) and the bottom \( T_u \) is zero. If the system is open, (i.e. it exchanges mass, momentum, energy and entropy with the environment) but sufficiently close to TE, there exists a unique steady state it will attain. Along this continuous set of steady states termed “thermodynamic branch”, linear relations between the system components dominate. In the reservoir (Fig. 1), this is associated with conductive heat transport, which is a linear function of the temperature gradient \( (T_u - T_o) \).
Along the thermodynamic path (including TE), systems invariably settle to a state of minimum Entropy Production (minEP) (Kondepudi and Prigogine, 1998). If an open system in steady state is, however, kept sufficiently far from TE (openness being, in fact, a precondition for this), nonlinear relations and cooperative micro-processes among system components can start to predominate, the thermodynamic branch can become unstable and, triggered by random micro-perturbations, bifurcations can lead to several branches of possible stable steady states. Sufficient distance from TE is hence a precondition for self-organisation to occur (see Sect. 4.2.1).

In the reservoir, self-organisation occurs in the form of convective cells if a critical temperature gradient \( dT_{\text{crit},1} \) is exceeded. All stable steady states after the point of instability of the thermodynamic branch are called “dissipative branch”, all systems along it “dissipative systems”, as here energy fluxes and energy dissipation are increased compared to systems on the thermodynamic branch. Increasing distance from TE is often associated with higher system structure (in Fig. 1 the existence of macroscopic convective cells) and stable dissipative systems typically settle to steady states of maximum Entropy Production (maxEP) as the most probable states (e.g. Dewar, 2005; Virgo, 2010).

Moving still further from TE, systems may reach further points of instability, in the case of the reservoir this is marked by a transition from convective to turbulent flow at \( dT_{\text{crit},2} \). The relation between the distance from TE, self-organisation associated with structure formation, accelerated dynamics and entropy production shown in Fig. 1 can also be applied to water flow through cohesive, erodible soils. Close to TE (here expressed by a small hydraulic gradient), diffusive water flow is linearly dependent on the hydraulic gradient. Beyond a critical hydraulic gradient, subsurface backward erosion can lead to the formation of (dissipative) preferential flow structures which accelerate the flow and add an entirely new quality to it. Most hydrological systems of interest can be viewed as dissipative structures, exchanging mass, energy and entropy with the environment, being kept far from TE by solar radiation or mantle convection (directly or indirectly), being composed of many sub-systems connected by highly nonlinear rela-
tions, exhibiting dissipative processes such as radiation, soil heat flow, frictional water flow, diffusion, photosynthesis. Thermodynamics therefore lends itself as a framework to deal with catchments as complex dynamical systems (Sect. 4.1), catchment self-organisation (Sect. 4.2.1) and co-evolution (Sect. 4.2.2).

So what does application of a thermodynamic perspective to hydrological systems actually imply? At a minimum, it comprises the definition of the system, i.e. its boundary and relevant sub-systems, keeping track of mass-, energy-, momentum- and entropy budgets while ensuring conservation of mass, energy and momentum and establishment of all relevant thermodynamic state variables. Further, all dynamics should be expressed on the basis of paired (conjugate) variables: the gradient of one of the two variables is depleted by the flux of the other; together they always describe a form of energy. For example, a gradient in geopotential fuels a mass flux, which eventually depletes the gradient. Together, mass [kg] and the gradient in geopotential [m² s⁻²] describe energy in the form of potential energy [J] (see also Kondepudi and Prigogine, 1998 or Kleidon, 2010). The direct benefit is that thus relating dynamics to the universal “currency” of energy provides a link between any kind of process, be it abiotic, biotic, or anthropogenic. Moreover, it puts emphasis on the role of feedbacks: Based on the above general form, fluxes are equal to a driving gradient divided by a resistance term, which is essentially a linear process. Nonlinearity then enters dynamics in the form of feedbacks: Any flux depleting its nourishing gradient is associated with a negative feedback, positive feedbacks can occur through local enhancement of the gradient (e.g. formation of locally steepened hill slopes which increase fluxes of water and sediment, Kleidon et al., 2013) or by local decrease of the resistance (e.g. by formation of low-friction drainage networks, Kleidon et al., 2013, or by the decreasing flow resistance of soil caused by wetting).

For prediction of catchments under change, an explicit representation of such feedbacks is vital, as for systems far from TE, it is the balance of positive and negative feedbacks that keeps them in or pushes them out of stable quasi-steady states. Further, expressing dynamics via a concept of cascading energy conversions along hierar-
chical thermodynamic gradients (see Fig. 2) leads to a natural hierarchy of processes which is useful, not only to establish hierarchical modeling concepts, but also to allow formulation of upper thermodynamic limits to the magnitude of each conversion process (see e.g. Kleidon and Renner, 2013). It is, however, important to understand that in this hierarchical view of earth system processes, the boundary conditions of each conversion process are not fixed and there may be strong interactions between dynamics and boundary conditions. For hydrologic fluxes in catchments this is e.g. reflected through evaporative fluxes, which (jointly with the sensible heat flux) deplete the vertical heating gradient between the heated surface and the cooled atmosphere (Kleidon and Renner, 2013).

4.3.1 Optimality principles

Analysis of non-equilibrium systems has led to the proposition of extremum or optimality principles such as minEP (see above) and maxEP (Paltridge, 1978; Ozawa et al., 2003; Kleidon and Lorenz, 2005; Dewar, 2005), which direct their development towards final steady states. For transient dissipative systems with many degrees of freedom, they can therefore be used as “selection criteria” distinguishing more and less probable pathways of development. MaxEP, for example was proposed for prediction of the partitioning of water between evapo-transpiration and runoff (Kleidon and Schymanski, 2008) and was used to predict effective global transfer coefficients for root water uptake and base flow (Porada et al., 2011), and for the effects of vegetation banding on aggregated biomass and water fluxes (Schymanski et al., 2010).

Closely related to maxEP, it has recently been suggested that dissipative systems develop such that the time to reach TE is minimized, or in other words that work done over time (power) by the system is maximized (maximum Power Principle maxP, Kleidon, 2010; Kleidon et al., 2013). Recently, Zehe et al. (2012) have shown that the choice of macroporosity as optimal with respect to maxP has allowed calibration-free reproduction of observed hillslope hydrological dynamics. Optimality principles can thus reduce data demands and the need for calibration, which is especially useful for transient or
ungauged catchments. Many other optimality principles have been proposed, such as maximisation of gross or net primary productivity to predict biomass dynamics or maximum net carbon profit to predict vegetation water use (Schynamski et al., 2009). It has been suggested, however, that upon choosing system extent and scale of consideration appropriately, many can be translated to maxEP (Dewar, 2010).

Disturbance of steady-state dissipative systems can either leave them unaffected or cause build-up or decay of structure, depending on the system’s position on the dissipative branch (proximity to points of instability, see Fig. 1) and the strength and nature of the disturbance. Viewing catchments under change as complex, dynamical (see Sect. 4.1) and dissipative systems can therefore provide a framework to evaluate their stability, resilience and predictability. Last but not least, adding energy considerations to the analysis and prediction of hydrological systems offers additional observables which can help to better determine system dimensionality and to represent and constrain system dynamics.

4.4 Catchments as sources and flow paths of information

The next perspective we take is that of information theory. It focuses on the way how information is extracted from data, how it can be compressed and stored, and its relation to uncertainty. As “information” is a universal quantity, information theory is a potentially useful framework in which the information content, for a given purpose, across data, scientific laws, model structures or model parameters can be evaluated. Its primary value with respect to addressing questions of change is therefore not so much in its direct application to such problems, but rather by providing a basis for the evaluation and improvement of predictive models. “Information” can be viewed as a quantity that connects processes and quantities in the real world with conceptual representations of those processes and quantities in our minds, or in computers. To understand this, note that “observation” consists of a process by which attention to a quantity under investigation brings about some kind of change of state – in a brain this can be a change in potential level of one or more neurons, and in a computer this can be the change in
value of a bit within memory. Arguably, all of the knowledge accumulated about a catchment eventually stems from observations, and this then provides the information upon which our mental and computer models are based.

As mentioned earlier in Sect. 2, all observations about reality are converted into representations of knowledge by a process of “explanation”, which can be viewed as a form of compression (Weijs et al., 2013a) in which a compact conceptual and/or mathematical description is used to describe/represent the structures that underlie the co-variation seen to exist in the observations. If enough observations are present, if the noise in the observations is not too large, and if the underlying structure is sufficiently strong and unchanging (i.e. consistent co-variation among the variables actually exists), then these compact descriptions will represent any relevant structure in the data and therefore most likely describe the general laws that can be deduced from the observations. These descriptions will then allow the transfer of relevant information contained within those observations, to other, sufficiently similar situations, thereby allowing the values of unobserved quantities to be predicted and decisions to be made regarding our interactions with the real system.

4.4.1 Representing information and its role in the reduction of uncertainty

Although important foundations were laid earlier, the birth of Information theory is mainly attributed to the seminal paper by Shannon (1948), who defined information and uncertainty as quantities that can be represented in terms of discrete values known, for example, as bits (binary integers). More specifically, uncertainty or missing information is viewed as being connected to the process of “choice” (decision making) and is represented in terms of the probabilities associated with different possible outcomes of an event. For events that can take on a discrete number “n” of possible outcomes \(i = 1, \ldots, n\), the measure for uncertainty, called information entropy \((H)\), is defined as the expected value of the negative log-probability \(-\log_b P(i)\) of those outcomes, given as (there is also an analogous definition for continuous variables):
\[ H = E\{-\log_b P(i)\} = \sum_{i=1}^{n} -\log_b P(i) \cdot P(i) \]  

Since anything that contributes to our knowledge/understanding about the value of an event can be thought of contributing to a change in our prior state of uncertainty about the value of that event, a gain in information can be defined as a reduction in uncertainty (Cover and Thomas, 2006). Alternatively, when observing an event, the gain in information can be equated to the “surprisal” caused (i.e., the extent to which the new information is unexpected, or changes our expectation about the value of the event), which was defined by Shannon to be \(-\log_b P(i)\), where \(b\) can be chosen in some convenient fashion. Therefore, the entropy \(H\) can be interpreted as the “expected surprise” about the true outcome.

Of course, in a more general sense, the probabilities referred to above can be thought of as reflecting states of knowledge (instead of just representing frequencies of occurrence), and we can adopt a more general (Bayesian) view in which probability distributions are used to represent carriers of (incomplete) information, and in which the axioms of probability function as the rules for logical reasoning (Jaynes, 2003). In this more general case, it is important to recognize that information can also be wrong (i.e., bad) in the sense that it can result in an increase in uncertainty about the true outcome.

### 4.4.2 Applying concepts of information theory to catchment hydrology – potential and limitations

Information theory provides a formal framework for linking observations, laws, models, and computerized algorithms. It therefore has the potential to play an important part in a theory of evaluation (Gupta et al., 1998, 2008, 2012) that facilitates a robust evaluation and improvement of model performance (Gong et al., 2013), and in the evaluation of models of different degrees of complexity as in the case of multiple working hypotheses (Solomonoff, 1964; Clarke et al., 2011). Information theory also can provide...
a framework to optimize strategies of data collection (Alfonso et al., 2010; Mishra and Coulibaly, 2010; Li et al., 2012; Gupta et al., 2013a) and data assimilation (Nearing, 2013) in catchment hydrology. As information and uncertainty are closely linked (see Sect. 4.4.1), this framework is also potentially suited for quantification and minimization of uncertainty associated with decisions, e.g. in water resources management (Weijs et al., 2010) or choices of model structure (Nearing, 2013; Gong et al., 2013).

When applying information theory in practice, however, we should keep in mind that information theoretical quantities depend on probabilities, which in turn depend on states of (prior) knowledge. So results will depend importantly on our prior knowledge and how we choose to formalize it, which adds subjectivity and non-uniqueness to the processes of evaluation and prediction. For example, a time series of perfectly measured discharge contains, \( N \cdot H(Q) \) bits of information for specifying what the discharge is at every time step, where \( N \) is the length of the time series and \( H(Q) \) is the entropy of the suitably (subjectively depending on the question asked) binned discrete distribution (histogram) of \( Q \), but this assumes knowledge of the frequency distribution and no knowledge of or learning from temporal dependencies. When taking these dependencies into account, the information content is equal to the joint entropy of the entire series, and the frequency-based approach breaks down, since the joint entropy depends on an \( N \)-dimensional histogram with one observation. Alternatively, the joint entropy can be approximated by the conditional entropy of \( Q_t \), given \( Q_{t-L} \ldots Q_{t-1} \). This last quantity involves a model for predicting \( Q \) from its previous \( L \) time steps, with the model structure assumed to be known (e.g. Gong et al., 2013). Models of different complexity will give different answers. If the models are not known a priori, but inferred from the data, the model description length in bits should be added to the information content (Weijs et al., 2013a). Finally, in the hypothetical case that meteorological conditions and all hydrological processes are already perfectly known, the information content of the discharge series becomes zero, because the perfectly predictable values no longer contain any surprise.
To summarize, applying concepts of information theory to catchment hydrology does not eliminate subjectivity associated with the way we treat prior knowledge, but it forces us to be more explicit about it and about the way it affects our predictions and decisions.

5 Summary and conclusions

We started from the observation that the hydrological cycle is increasingly affected by changes, which extend from local to global scale, act on short to decadal time scales and affect all characteristics of water-related dynamics. Humans play a double role in this, as they cause many of these changes and are at the same time concerned by them, thus demanding answers regarding the hydrological effects of global change. These changes potentially push hydrological systems out of the quasi-steady states they have reached through long-term co-evolution of their constituents, giving rise to the interplay of feedback effects which determine the systems path towards new stable states. Hydrological concepts developed under stationary conditions may not capture all the mechanisms that are relevant under transient conditions.

Therefore, the main focus we have pursued in this article was to present and discuss paradigms and theories which we consider helpful to advance hydrology towards understanding and predicting hydrological systems under change. To this end, we started with a discussion of the general nature of explanation in hydrology, which is characterized by considerable pluralism stemming from different explanation types, the interdisciplinary nature of hydrology and underdetermination.

We continued by discussing the special characteristics of catchments, namely straightforward closure of the water balance due to convergence and existence of distinctly separate process scales for water flow and structure formation. Both have favoured development of simple, but successful sectoral hydrological models based on the assumption of stationarity, linear concepts and limited availability of observations. From this, we proposed several perspectives on catchments to deal with transient conditions (an overview is shown in Fig. 3): treating catchments as complex dynamical sys-
tems offers ways to classify them (Table 1) and to assess their stability, resilience and predictability. Looking at catchments from the point of view of the related field of synergetics highlights the occurrence of self-organization and emergence of macro-scale structures (spatial, temporal or functional). The advantage of exploiting such phenomena is that it greatly reduces the systems’ degrees of freedom to the number of order parameters, making predictions a more straightforward task. It can also help to explain the apparent similarity of many catchments.

The next viewpoint we adopted is that of catchments as co-evolving systems, focusing on the mutual historical evolution of catchment constituents, and learning from analysis of the similarities and dissimilarities of catchments that started from presumably similar conditions in the past (Fig. 3). This is closely related to the analysis of catchment similarities, and both can help to provide constraints on parameters of predictive models and to transfer information among catchments in “space-for-time” trading approaches.

The thermodynamic view of catchments focuses on stocks, fluxes, conversions and dissipation of energy. Treating catchments as open dissipative thermodynamic systems far from equilibrium offers a framework which explains both the fundamental tendency towards degradation of structure, but also the preconditions for its build-up, whose interplay plays an important role in the evolution of hydrological systems over time. The benefit of expressing dynamics in the universal “currency” of energy is that it provides a link between any kind of process, be it abiotic, biotic, or anthropogenic. Also, optimality principles formulated in the fundamental terms of energy and entropy can potentially be applied to direct the development and prediction of new stable states of systems under change.

Finally we took the perspective of information theory, which offers an alternative view on the nature of explanation (as data compression) and a general framework for the evaluation of information content (expressed in terms of the reduction of uncertainty about a target quantity of interest), across data, laws, and models. This makes it po-
potentially a useful part in a theory of evaluation that facilitates critical assessment and improvement of predictive models.

In their article on the nature of explanation in the earth sciences, Kleinhans et al. (2005) conclude that the best way to overcome underdetermination is a combination of historical actual-sequence explanations, robust process explanations and causal explanations in the form of laws. We adopt this view for hydrological systems, and especially hydrological systems under change, which is reflected in the previously proposed perspectives on catchments (see Fig. 3): Analysing catchment co-evolution provides insight into the historical development of actual catchments and potentially robust process explanations of the underlying mechanisms. Applying the methods of complex system analysis to catchments under change can provide general statements on predictability, and allows linkage of existing scale-specific hydrological laws, when seen as manifestations of emergent phenomena on different macroscopic scales. Expressing dynamics on the basis of the universal laws of thermodynamics facilitates linking all the processes involved in the hydrological cycle and allows formulation of constraints to its dynamics. Finally, the information-theoretic view is both helpful as a common framework for the many modeling approaches in hydrology, and has links to the self-organisation of systems (Kumar and Ruddell, 2010).

While the approaches we presented to deal with catchments under change are not new, and are in fact based on existing and well-established theories, we suggest that their synergistic combination can serve as a paradigm to direct the further development of catchment hydrology to address questions of change.

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Table 1. Classification of dynamical systems (simplified from Strogatz, 1994, p. 10, Fig. 1.3.1).

<table>
<thead>
<tr>
<th></th>
<th>Number of variables</th>
<th>Continuum</th>
</tr>
</thead>
<tbody>
<tr>
<td>( n = 1 )</td>
<td>( n = 2 )</td>
<td>( n \geq 3 )</td>
</tr>
<tr>
<td>Linear</td>
<td>Growth and decay</td>
<td>Oscillations</td>
</tr>
<tr>
<td></td>
<td>Radioactive decay</td>
<td>2-body problem</td>
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<td></td>
<td></td>
</tr>
<tr>
<td>Nonlinear</td>
<td>Fixed points</td>
<td>Pendulum</td>
</tr>
<tr>
<td></td>
<td>Bifurcations</td>
<td>Anharmonic oscillators</td>
</tr>
<tr>
<td></td>
<td>Overdamped system</td>
<td>3-body problem</td>
</tr>
<tr>
<td></td>
<td>Logistic equations</td>
<td>Fractals</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Forced nonlinear</td>
</tr>
<tr>
<td></td>
<td></td>
<td>oscillation</td>
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<tr>
<td></td>
<td></td>
<td>Strange attractors</td>
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<tr>
<td></td>
<td></td>
<td>3-body problem</td>
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<td></td>
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<td>Fractals</td>
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<td></td>
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<td>Forced nonlinear</td>
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<td>Laizers</td>
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<td></td>
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<td>Nonequilibrium statistical</td>
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<td></td>
<td></td>
<td>mechanics</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Nonlinear solid-state</td>
</tr>
<tr>
<td></td>
<td></td>
<td>physics</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Ecosystems</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Nonlinear waves</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Turbulent fluids</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(Navier–Stokes)</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Reaction-diffusion</td>
</tr>
<tr>
<td></td>
<td></td>
<td>biological and chemical</td>
</tr>
<tr>
<td></td>
<td></td>
<td>waves</td>
</tr>
</tbody>
</table>
Table 2. List of definitions (alphabetical order).

<table>
<thead>
<tr>
<th>Definition</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Co-evolution</td>
<td>Joint evolution (see also “evolution”) of several interacting components (abiotic and/or biotic) of a system. Biological co-evolution is the joint biological evolution of two species connected by conflicts or cooperation.</td>
</tr>
<tr>
<td>Evolution</td>
<td>In this article we adopt the general meaning of evolution as gradual development of something. This can include the special case of biological evolution, which is characterized by natural selection leading to adaptation, speciation, divergence or extinction of species on the basis of inheritance, random mutation and recombination of genetic information.</td>
</tr>
<tr>
<td>Forecast</td>
<td>Quantitative prediction for a given location at a specified future time.</td>
</tr>
<tr>
<td>Non-steady state</td>
<td>No change of structure over time, but state variables and fluxes (within the system and across its borders) do change.</td>
</tr>
<tr>
<td>Paradigm</td>
<td>Worldview or code of practice commonly accepted in a scientific field at a given time. It guides both the kind of questions (experiments, observations) that are being asked in a scientific field as well as the way the results are interpreted (e.g. Kuhn, 1970). It can include several scientific theories.</td>
</tr>
<tr>
<td>Prediction</td>
<td>Approximating an unknown state of a system with full, partial or no knowledge of initial and boundary conditions. In statistical terms it is the approximation of the actual but unknown realization of a stochastic variable.</td>
</tr>
<tr>
<td>Projection</td>
<td>Prediction of a possible future state of a system under certain assumptions (e.g. assumption of an emission scenario in climate projections). A projection hence cannot be associated with an occurrence probability.</td>
</tr>
<tr>
<td>Quasi-steady state</td>
<td>Steady state for long (aggregation) time scales (steady state of long-term mean states and fluxes), but non-steady state for shorter time scales. See also “steady state”.</td>
</tr>
<tr>
<td>Scientific law</td>
<td>Statements on causal relations among its constituents, exceptionless and irreducible within its scope (system, scale, boundary conditions). Laws are based on empirical evidence, can often be expressed by mathematical equations and hence be used in computer models.</td>
</tr>
<tr>
<td>Scientific theory</td>
<td>Explanation of some aspect of the natural world, established by following the scientific method and confirmed by observation and experiment (empirical evidence). A theory has explanatory and predictive power; its strength is related to the parsimony of its principles, the diversity of phenomena it can explain and the quality of its falsifiable predictions (e.g. Popper, 2002). It can contain several scientific laws.</td>
</tr>
<tr>
<td>Stationary state</td>
<td>In this text used interchangeably with steady state. In statistical terms: The underlying distribution of a random variable does not change with time.</td>
</tr>
<tr>
<td>Steady state</td>
<td>No change of structure, states and net fluxes (within the system and across its borders) over time, at least one flux is non-zero. See also “quasi-steady state” and “stationary state”.</td>
</tr>
<tr>
<td>Thermodynamic equilibrium (TE)</td>
<td>No change of structure, states and fluxes (within the system and across its borders) over time, all fluxes are zero.</td>
</tr>
<tr>
<td>Transient state</td>
<td>State of a system that undergoes structural changes over time.</td>
</tr>
</tbody>
</table>
Fig. 1. Highly simplified sketch of steady state heat transport and entropy production (dissipation) in a reservoir heated at the bottom, as a function of distance from thermodynamic equilibrium (TE). The distance from TE is expressed by the temperature difference between bottom and top. Beyond a critical distance from TE, self-organisation creates macroscopic structure (convective cells, turbulence), accelerating the heat flux from bottom to top.
Fig. 2. Simplified summary of a hierarchy of power transfer among Earth system processes. Solid arrows describe flows of energy, while dotted arrows describe effects. From Kleidon (2010).
Fig. 3. Overview and connection of the paradigms discussed in the paper to improve hydrological predictions under change.